

## 1 List'em all!

List all the asymptotic runtimes from quickest to slowest.

$\theta(n^2)$ ,  $\theta(n^{0.5})$ ,  $\theta(\log n)$ ,  $\theta(3^n)$ ,  $\theta(c)$ ,  $\theta(n^n)$ ,  $\theta(n)$ ,  $\theta(n \log n)$ ,  $\theta(n!)$ ,  $\theta(n^n)$ ,  $\theta(2^n)$

**Solution:**  $\theta(c)$ ,  $\theta(\log n)$ ,  $\theta(n^{0.5})$ ,  $\theta(n)$ ,  $\theta(n \log n)$ ,  $\theta(n^2)$ ,  $\theta(2^n)$ ,  $\theta(3^n)$ ,  $\theta(n!)$ ,  $\theta(n^n)$ ,  $\theta(n^n)$

## 2 What's that runtime?

For each of the methods below, please specify the runtime in BigO, Big $\Theta$  or Big $\Omega$  Notation. Please give the tightest bound possible.

**Solution:**  $\theta(n^3)$ , the  $i$  loop runs  $n$ , the  $j$  loop runs  $n$ , each time doing a function that takes  $n$ , so  $n * n * n = n^3$ .

```
_____ private static void f(int n) {
        for(int i = 0; i < n; i++) {
            for(int j = 0; j < n; j++) {
                linear(n); // runs in linear time with respect to input
            }
        }
    }
```

**Solution:**  $\theta(n \log n)$ ,

```
_____ private static void g(int n) {
        if (n < 1) return;
        for(int i = 0; i < n; i++) {
            linear(100);
        }
        g(n/2);
        g(n/2);
    }
```

**Solution:**  $O(n)$

```
private static void h(int n) {
    Random generator = new Random();
    for(int i = 0; i < n; i++) {
        if(generator.nextBoolean()) {
            /* nextBoolean returns true with
            probability .5. */
            break;
        }
    }
}
```

### 3 How fast?

Given a IntList of length  $N$ , provide the runtime bound for each operation. Recall that IntList is the naive linked list implementation from class.

Operations	Runtime
size()	$\theta(N)$
get(int index)	$O(N)$
addFirst(E e)	$\theta(1)$
addLast(E e)	$\theta(N)$
remove(int index)	$O(N)$
remove(Node n)	$O(N)$

## 4 The ABCs of OOP

Indicate what each line the main program in class **D** would print, if the line prints anything. If any lines error out, identify the errors as compile-time or runtime errors and cross out the corresponding lines.

```
public class A {  
    public void x() { System.out.println("Ax"); }  
    public void y(A z) { System.out.println("Ay"); }  
}
```

```
public class B extends A {  
    public void y() { System.out.println("By"); }  
    public void y(B z) { System.out.println("Byz"); }  
}
```

```
public class C extends A {  
    public void x() { System.out.println("Cx"); }  
}
```

```
public class D {  
    public static void main(String[] args) {  
        A e = new B();  
        A f = new C();  
        B g = new A(); Solution: Compile-Time Error. A is not a sub-  
class of B  
        B h = new C(); Solution: Compile-Time Error. Although B and  
C are are both children classes of A, B and C are not related to each other.  
        C i = (C) new A(); Solution: Runtime Error. Casting would trick  
the compiler to think of the new object as type C and then assign it to i.  
While running the program, casting will crash because the new object is type  
A in dynamic binding, which cannot be assigned to class C (as A is not a  
subclass of C).  
        B j = (A) new C(); Solution: Compile-Time Error. Casting will  
trick the compiler to think of the new object as type A. However in run-  
time when looking at the dynamic types, we cannot assign it to type B since  
A is not a subclass of B.  
        B k = (B) e; Solution: e is type B in dynamic type, so the as-  
signment works out fine in run-time.
```

f.x(); **Solution:** Cx

e.x(); **Solution:** Ax

e.y(); **Solution:** Compile-Time Error. e is treated as an object under class A when compiling. Class A doesn't have the y method whose input is empty.

(B) e.y(); **Solution:** Compile-Time Error. This attempts to cast the value returned by e.y() to B, rather than actually casting e to type B. Therefore this does nothing to fix the issue described in the above part.

((B) e).y(); **Solution:** By

e.y(e); **Solution:** Ay

e.y(f); **Solution:** Ay

}

## 5 Classy Cats

Look at the Animal class defined below.

```
public class Animal {
    protected String name, noise;
    protected int age;

    public Animal(String name, int age) {
        this.name = name;
        this.age = age;
        this.noise = "Huh?";
    }

    public String makeNoise() {
        if (age < 2) {
            return noise.toUpperCase();
        }
        return noise;
    }

    public String greet() {
        return name + ": " + makeNoise();
    }
}
```

- (a) Given the Animal class, fill in the definition of the Cat class so that it makes a "Meow!" noise when greet () is called. Assume this noise is all caps for kittens, i.e. Cats that are less than 2 years old.

**Solution:**

```

public class Cat extends Animal {
    public Cat(String name, int age) {
        super(name, age);
        this.noise = "Meow!";
    }
}

```

**Solution:** Inheritance is powerful because it allows us to reuse code for related classes. With the `Cat` class here, we just have to re-write the constructor to get all the goodness of the `Animal` class.

Why is it necessary to call `super(name, age);` within the `Cat` constructor? It turns out that a subclass's constructor by default always calls its parent class's constructor (aka a super constructor). If we didn't specify the call to the `Animal` super constructor that takes in a `String` and a `int`, we'd get a compiler error. This is because the default super constructor (`super();`) would have been called. Only problem is that the `Animal` class has no such zero-argument constructor!

By explicitly calling `super(name, age);` in the first line of the `Cat` constructor, we avoid calling the default super constructor.

Similarly, not providing any explicit constructor at all in the `Cat` implementation would also result in code that does not compile. This is because when there are no constructors available in a class, Java automatically inserts a no-argument constructor for you. In that no-argument constructor, Java will then attempt to call the default super constructor, which again, does not exist.

Also note that declaring a `noise` field at the top of the `Cat` class would not be correct. Since in Java, fields are bound at compile time, when the parent class's `makeNoise()` function calls upon `noise`, we will receive "Huh?". Because of this confusing subtlety of Java, which is called field hiding, it is generally a bad idea to have an instance variable in both a superclass and a subclass with the same name.

- (b) "Animal" is an extremely broad classification, so it doesn't really make sense to have it be a class. Look at the new definition of the `Animal` class below.

```

public abstract class Animal {
    protected String name;
    protected String noise = "Huh?";
    protected int age;

    public String makeNoise() {
        if (age < 2) {

```

```

        return noise.toUpperCase();
    }
    return noise;
}

public String greet() {
    return name + ": " + makeNoise();
}

public abstract void shout();
abstract void count(int x);
}

```

Fill out the `Cat` class again below to allow it to be compatible with `Animal` (which is now an abstract class) and its two new methods.

**Solution:**

```

public class Cat extends Animal {
    public Cat() {
        this.name = "Kitty";
        this.age = 1;
        this.noise = "Meow!";
    }

    public Cat(String name, int age) {
        this();
        this.name = name;
        this.age = age;
    }

    @Override
    public void shout() {
        System.out.println(noise.toUpperCase());
    }

    @Override
    void count(int x) {
        for(int i = 0; i < x; i++) {
            System.out.println(makeNoise());
        }
    }
}

```

**Solution:** To override an abstract method, the method signature's access modifiers must match exactly. Since `shout` is declared to be `public abstract` in `Animal`, our `Cat` class must declare it to be `public` to ensure that access modifiers match. The default access modifier for abstract classes is the same as the default access modifier for regular Java classes. Since `count` has the default access modifier in the `Animal` abstract class, `count` has the default access modifier when we override it in the `Cat` class.