DATA 8
Spring 2021

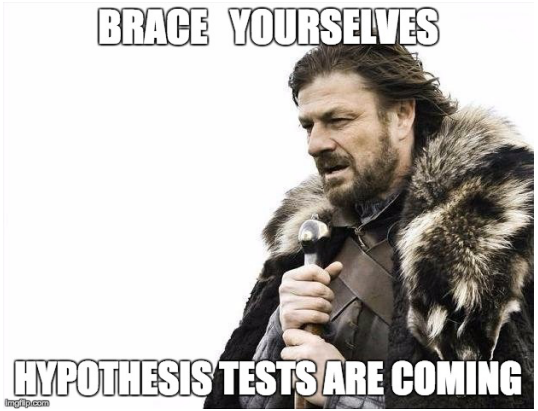
Discussion 7

Assessing Models

Materials: tinyurl.com/d8-disc07
or access through kevin-miao.com under teaching

Today

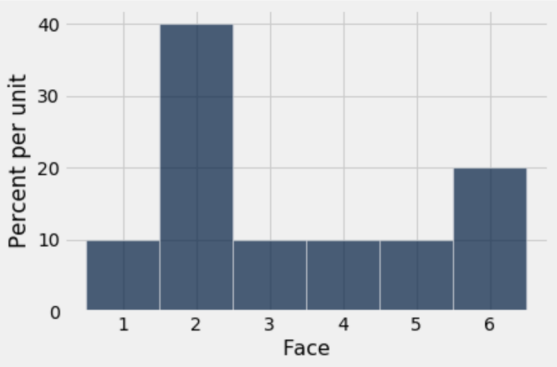
- Announcements
- Review: Testing Models
- Worksheet
  - Link: www.tinyurl.com/d8-disc07

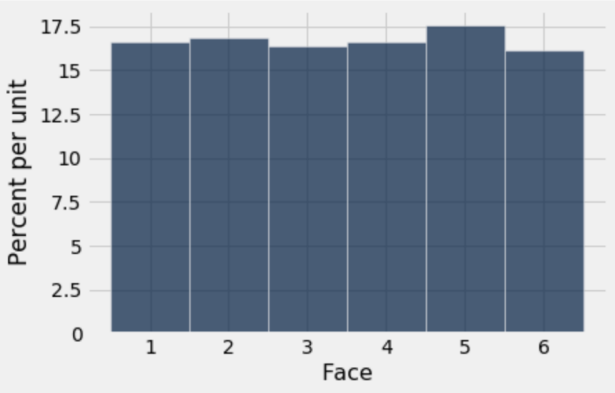


Announcements

- **Discussion Attendance Points**
- All office hours have been converted to group settings
- Assignments:
  - **Vitamin 6** is due tonight
  - **Homework 6** is due Thursday
- **Regrades** for homework 4, vitamin 5 and lab 5 **due Friday**
  - Gradescope: Submit regrade via button
  - OkPy: Email me
- *Informal OH:* Feel free to stay after discussion until 9:30am, if you have homework/project/course related questions.

🎲 Law of Large Numbers





Testing Models

Scenario:
We know a fair coin has ½, ½ probability landing tails and head. Given a coin and flip it 10 times (we don't know if it is fair or not), we see it lands heads 7 times. Is this possible with a fair coin? Is this possible with a biased coin?

Hypothesis testing allows us to simulate a fair coin and formalize this problem into a procedure.

Hypothesis Testing

- **Objective:** We want to see whether it is likely that a coin is fair, given that we know it lands heads 7 times, for instance.
- **Concretely**: We want to use simulations. We can only simulate a fair coin (i.e. we know that a fair coin lands heads/tails ½, ½ of the time).
- **Procedure**
  - Simulation Model (Null Model)
  - Alternative Model
  - Test Statistic
    - We need to (arbitrarily) create a statistic (formula) that is
      - **High** if it is close to the **alternative**
      - **Low** if it is close to the **simulation**
  - Simulate under the simulation
  - 🤦 Decide whether the coin is fair or biased (Later in the class)

But when do we decide the coin is fair or unfair?

To the worksheet! ✍️

tinyurl.com/d8-disc07

Data 8 Spring 2021
Discussion: Testing Models (Disc 07)

When we observe something different from what we expect in real life (i.e. four 3's in six rolls of a fair die), a natural question to ask is "Was this observed difference what we expect due to random chance? Or was it due to something other than random chance?"

Hypothesis testing allows us to answer that question in a scientific and consistent manner, using the power of computation and statistics to conduct simulations and draw conclusions from our data.

Question 1. Francie is flipping a coin. She thinks it is fair, but is not sure. She flips it 10 times, and gets heads 9 times.

She wishes to determine whether the coin was actually unfair, or whether the coin was fair and her result of 9 heads in 10 flips was by random chance.

a. What is a possible model that you can simulate under?

b. What is an alternative model for Francie's coin? You don't necessarily have to be able to simulate under this model.

c. What is a good statistic that you could simulate? Calculate that statistic for your observed data.
Hint: If the coin was unfair, it could be biased towards heads or biased towards tails.

d. Complete the function `flip_coin_10_times`, which takes no arguments and returns the absolute difference between the observed number of heads in 10 flips of a fair coin and the expected number of heads in 10 flips of a fair coin.

```
def flip_coin_10_times():
   probabilities = make_array(0.5, 0.5)
   proportions = sample_proportions(_____________________________)
   num_heads = ___________________________________________________
   return ________________________________________________________
```

e. How would you change `flip_coin_10_times` to use np.random.choice instead of sample_proportions?

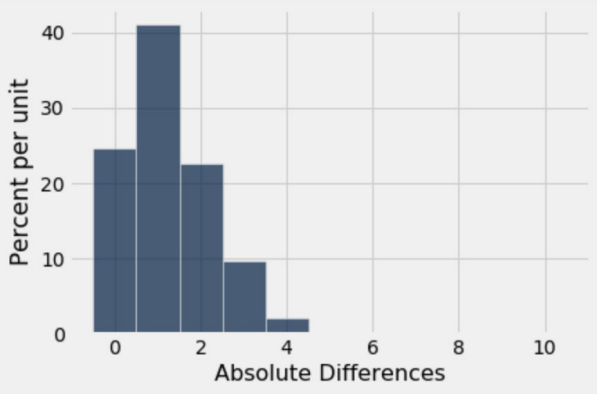
f. How would you change `flip_coin_10_times` to use .sample instead of sample_proportions?

g. Complete the code below to simulate the experiment 10000 times and record the statistic in each of those trials in an array called `abs_differences`.

```
trials = ____________________________________________________________
abs_differences = ___________________________________________________

for ___________________________________:
    abs_diff_one_trial =
    ____________________________________________
    abs_differences =
    ________________________________________________
```

h. Suppose we performed the simulation and plotted a histogram of `abs_differences`. The histogram is shown below.



Is the observed statistic described in the question consistent with the model we simulated under?

Question 2. As a student fed up with waiting times at office hours, you scout out the number of people in office hours (OH) from 11-12, 12-1, and 1-2 in B6 Evans. The Head GSI claims that the distribution of students is even across the three times, but you do not believe so. You observe the following data:

OH Time	Number of Students
11-12	250
12-1	300
1-2	200

Being a cunning Data 8 student, you would like to test the Head GSI's claim. Before you design your test, consider: <u>are office hour times numerical data or categorical data?</u>

a. What is the Head GSI's hypothesis?

b. What is the student's hypothesis?

c. Which hypothesis (Head GSI or student) can you simulate under?

d. What is a good statistic to use? *Hint: What is a good statistic for measuring the distance between two categorical distributions?*

End of Section

How did I do?

https://tinyurl.com/kevind8feedback